

# 國立虎尾科技大學 110 學年度第 1 學期博士班資格考試題

系別：動力機械工程系機械與機電工程博士班

Page 1 / 2

科目：機構學 Mechanisms

注意事項：

- (1) 本試題共有 6 題，合計 100 分。
- (2) 請依序作答於答案卷上並註明題號，若未註明選答題號及超過規定題數時，謹採計作答順序較前之題目計分。
- (3) 可使用計算機 close book

1. There are 9 kinematic pairs shown in Fig. 1. (a). What kinematic pairs have 1 degrees of freedom? (b). What kinematic pairs have 2 degrees of freedom? and (c). What kinematic pairs have 3 degrees of freedom? (15%)

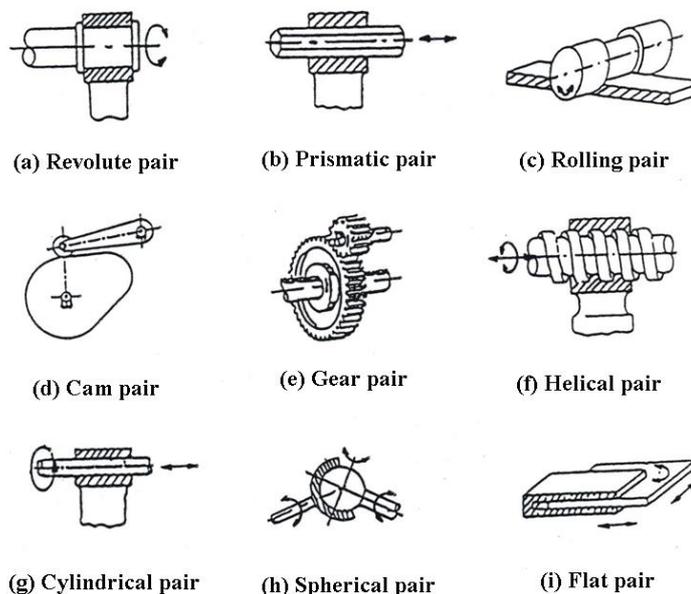


Fig. 1. The kinematic pairs of mechanism

2. Determine the mobility (number of degrees of freedom) of the following mechanical devices shown in Fig.2. (15%)

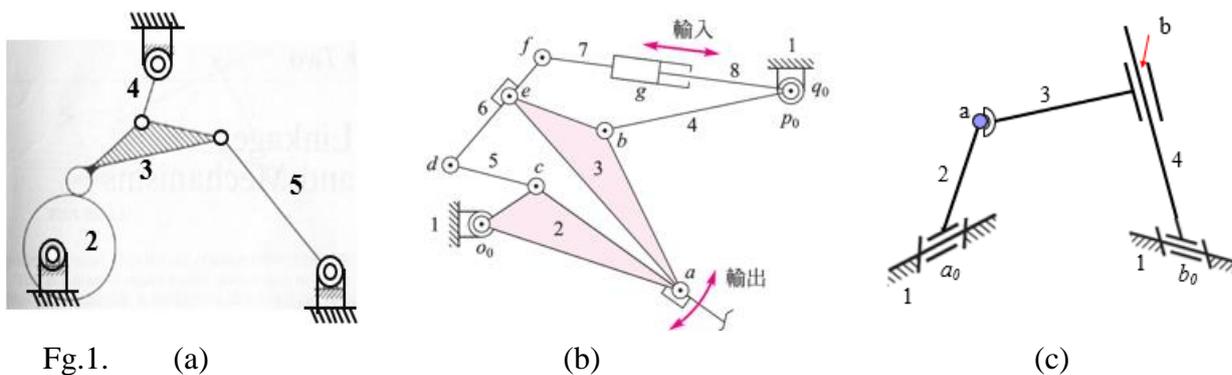


Fig.1. (a)

(b)

(c)

3. For the 4-bar mechanism shown in Fig. 3, crank 2 is to rotate continuously and link 4 is to oscillate. What are the maximum and minimum values in millimeters which can be used for the coupler length ( $l_3$ ). (20%)

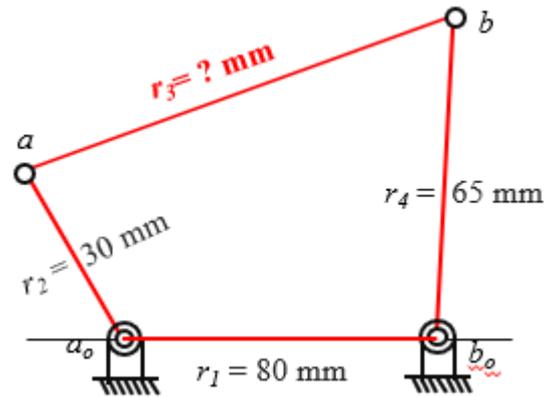


Fig. 3. 4-bar mechanism

4. For the 4-bar mechanism, shown in Fig. 3, with  $r_1=70\text{cm}$ ,  $r_2=30\text{cm}$ ,  $r_3=95\text{cm}$ , and  $r_4=65\text{cm}$ . When  $\theta_2 = 120^\circ$  and  $\omega_2=1200\text{rpm}$ , please find (a) the angular displacements of  $\theta_3$  and  $\theta_4$ , (b) the angular velocities of  $\omega_3$  and  $\omega_4$ . (20%)
5. A 2.5-module,  $25^\circ$  pinion of 18 teeth drives a 72-teeth gear. Calculate the pitch radii, base radii, addendum, dedendum, tooth thickness on the pitch circle, and the contact ratio. (15%)
6. For the planetary gear train shown in Fig. 4, gear 2 rotates at 600rpm in the clockwise direction. Calculate the output speed and direction of rotation of gear 5. (15%)

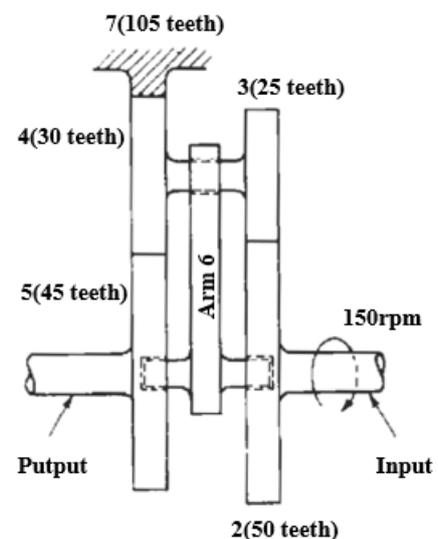


Fig. 4. A planetary gear train

# 國立虎尾科技大學 109 學年度第 2 學期博士班資格考試題

系別：動力機械工程系機械與機電工程博士班

第 1 頁 共 5 頁

科目：機構學

注意事項：

(1) 本試題共有 5 題，每題 20 分，合計一百分。

(2) 請依序作答於試題卷上。

(3) 可使用計算機 close book and can use calculator

1. Determine the mobility (number of degrees of freedom) of the following mechanical devices shown in Fig.1.

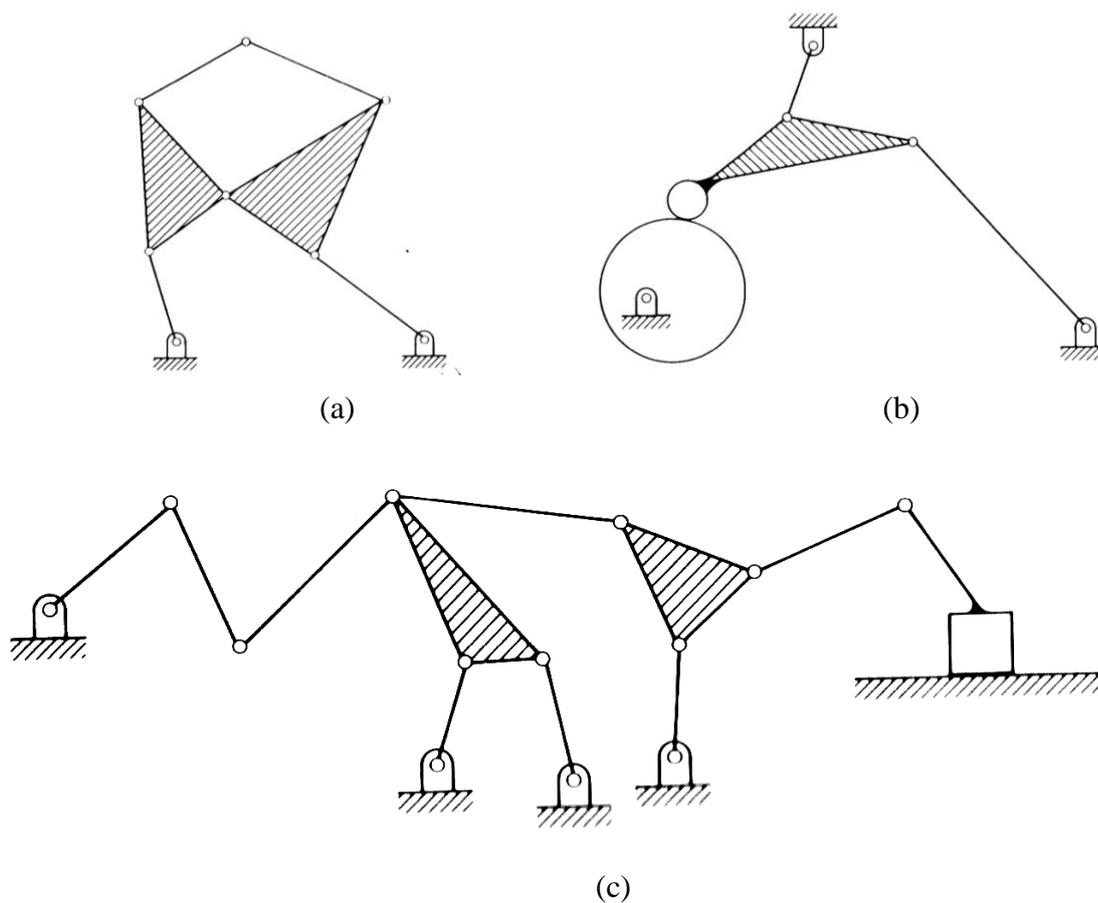


Fig. 1 Some mechanical devices

2. Consider the slider-crank mechanism shown in Fig. 2, derive the equations for the displacement ( $r_4$ ), velocity ( $v_4$ ), and acceleration ( $a_4$ ) of the slider. ( $\omega_2$  is constant)

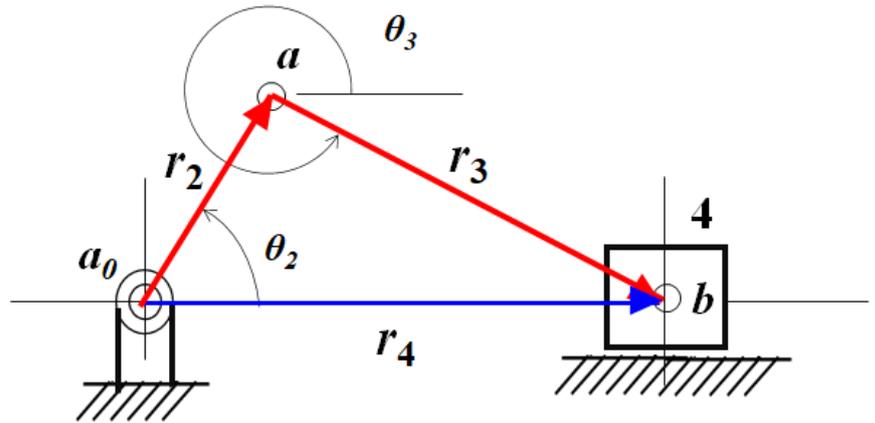


Fig. 2 Slider-crank mechanism

3. For the 4-bar mechanism shown in Fig. 3, crank 2 is to rotate continuously and link 4 is to oscillate. What are the maximum and minimum values in millimeters which can be used for the coupler length ( $l_3$ ).

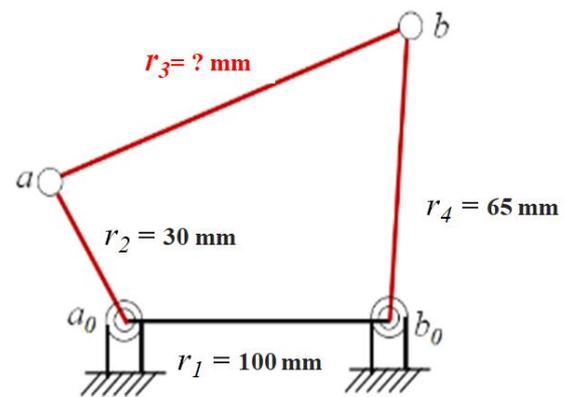


Fig. 3 4-bar mechanism

4. A 3-module,  $20^\circ$  pinion of 18 teeth drives a 45-teeth gear. Calculate the pitch radii, base radii, addendum, dedendum, tooth thickness on the pitch circle, and the contact ratio.

5. In the planetary gear train shown in Fig. 4, gear 2 rotates at 600rpm in the direction shown and gear 1 (and gear 6) rotates at 300rpm in the opposite direction. Calculate the speed and direction of rotation of gear 7.

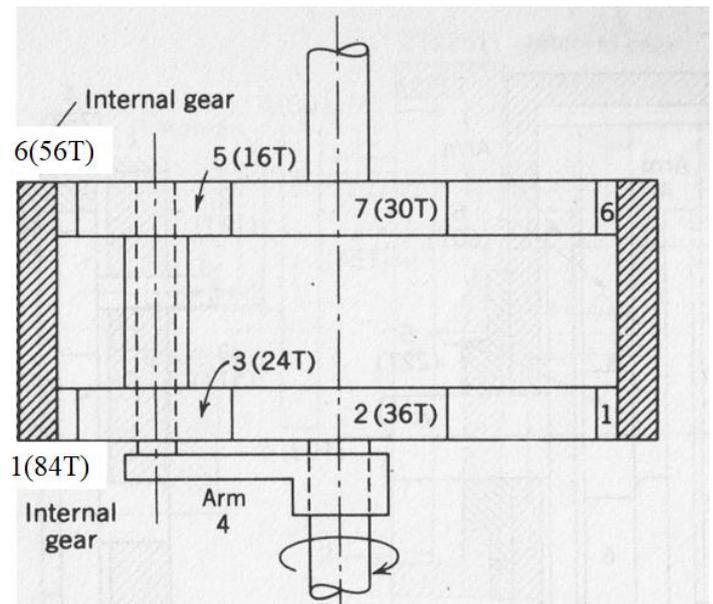


Fig. 4 A planetary gear train

國立虎尾科技大學 109 學年度第 1 學期博士班資格考試題

系別：動力機械工程系機械與機電工程博士班  
 科目：機構學

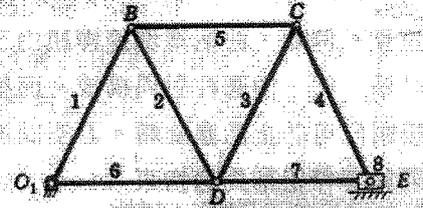
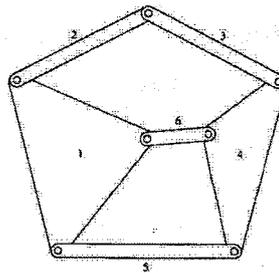
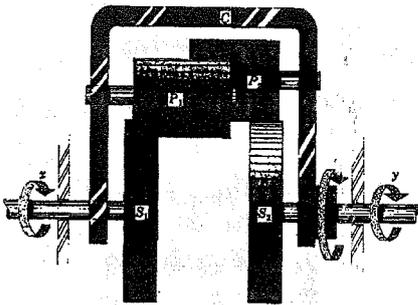
第 1 頁 共 3 頁

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- (3) 可以使用計算機並且可以攜帶一張 A4 大小之筆記(Bring engineering calculator and 1 page of A4 size note)

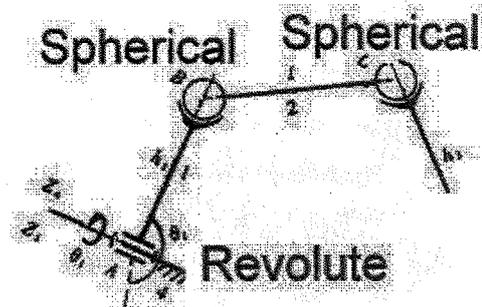
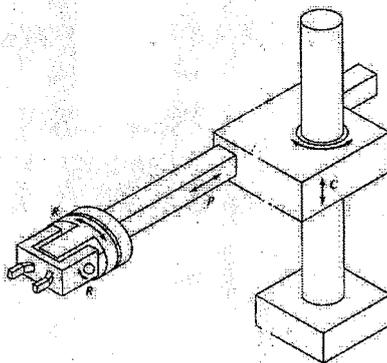
1. Please use Grubler equation to determine the mobility (number of degrees of freedom) of the devices shown in Figs. (a) through (e). (20%)

(a) Spur-Gear Differential      (b) Watt Six-Bar Linkage      (c) Truss



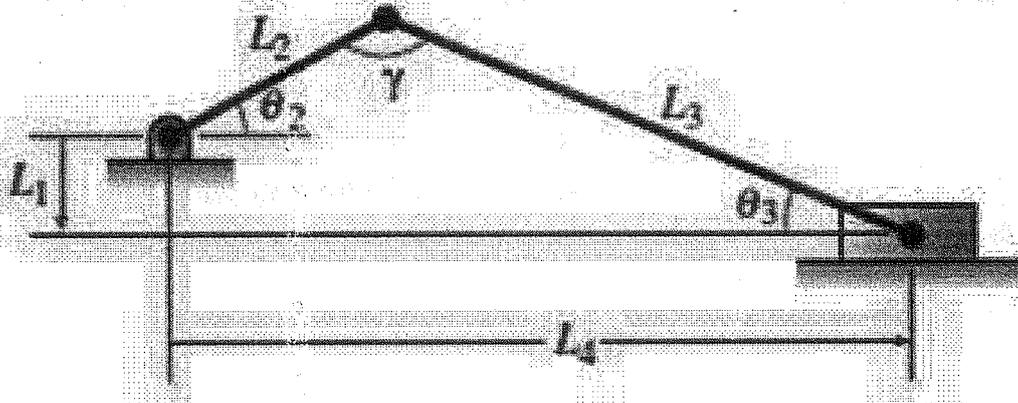
(d) Industrial Robotics

(e) Spatial Mechanism

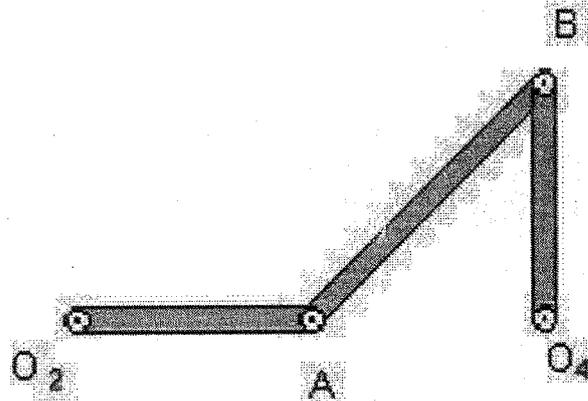


2. In the offset crank slider mechanism shown in the figure below the constrained path of the pin on the slider does not extend through the

center of rotation of the crank. Given the lengths  $L_1$ ,  $L_2$  and  $L_3$  and the crank angle  $\theta_2$ . Please determine (a) The interior joint angle  $\gamma$  and (b) The position of the slider  $L_4$ . (20%)

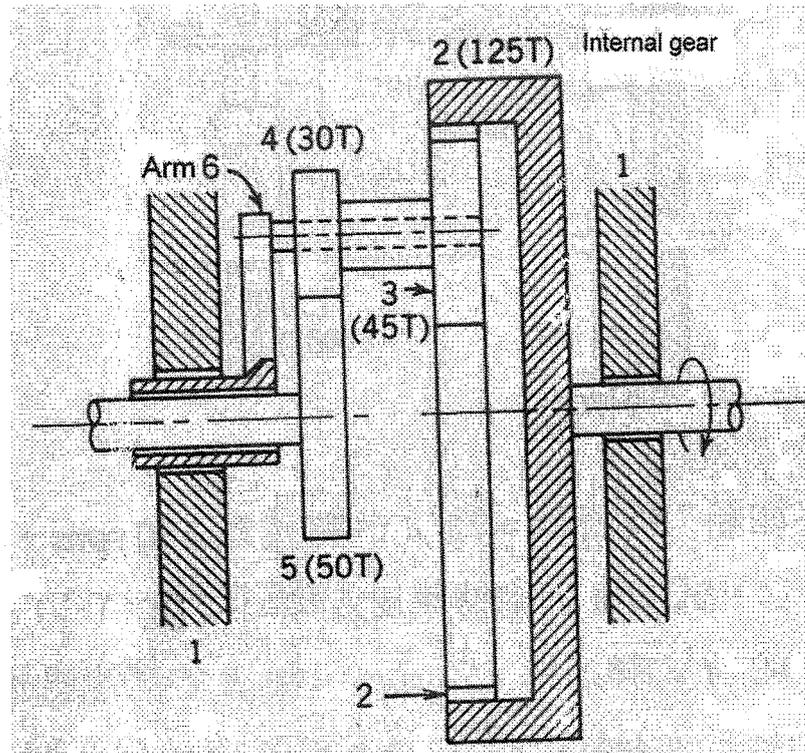


3. For the 4-bar linkage shown in the figure below, Link2 ( $O_2A$ ) rotates with the angular velocity  $\omega_2=10$  rad/s (CCW) and angular acceleration  $\alpha_2=10$  rad/s<sup>2</sup>. Given the lengths  $O_2O_4=2$ m (Link1: Fixed),  $O_2A=1$ m (Link2),  $O_4B=1$ m (Link4), and Link2 ( $O_2A$ ) overlaps with Link1 ( $O_2O_4$ ), Link4 ( $O_4B$ ) is perpendicular to Link1 ( $O_2O_4$ ). Please use any analytical method to calculate the angular velocities  $\omega_3$  and  $\omega_4$ , and the angular accelerations  $\alpha_3$  and  $\alpha_4$  of Link3 (AB) and Link4 ( $O_4B$ ). (20%)



4. A 2-module,  $20^\circ$  pinion of 24 teeth drives a 40 teeth gear, calculate the pitch diameter, base radii, dedendum, addendum, tooth thickness on the pitch circle, circular pitch, length of action and the contact ratio. (20%)

5. In the planetary gear train shown in the Figure below, gear 2 turns at 600 rpm in the direction indicated. Determine the speed and direction of rotation of arm 6 if gear 5 rotates at 350 rpm in the same direction as gear 2. (20%)



國立虎尾科技大學 108 學年度第 2 學期博士班資格考試題

系別：動力機械工程系機械與機電工程博士班

第 1 頁 共 3 頁

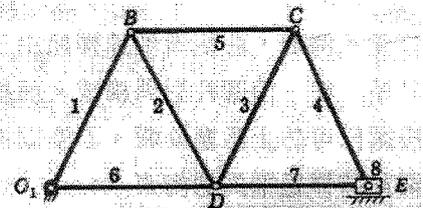
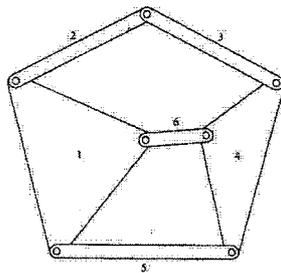
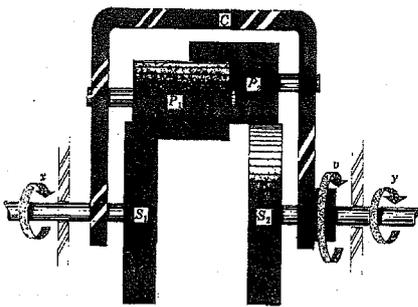
科目：機構學

注意事項：

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- (3) 可以使用計算機並且可以攜帶一張 A4 大小之筆記(Bring engineering calculator and 1 page of A4 size note)

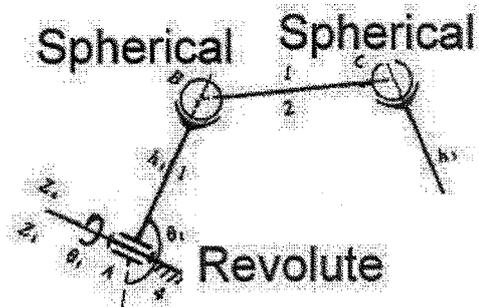
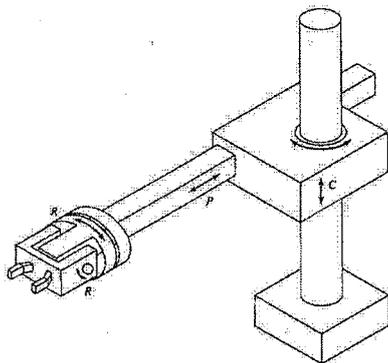
1. Please use Grubler equation to determine the mobility (number of degrees of freedom) of the devices shown in Figs. (a) through (e). (20%)

(a) Spur-Gear Differential      (b) Watt Six-Bar Linkage      (c) Truss



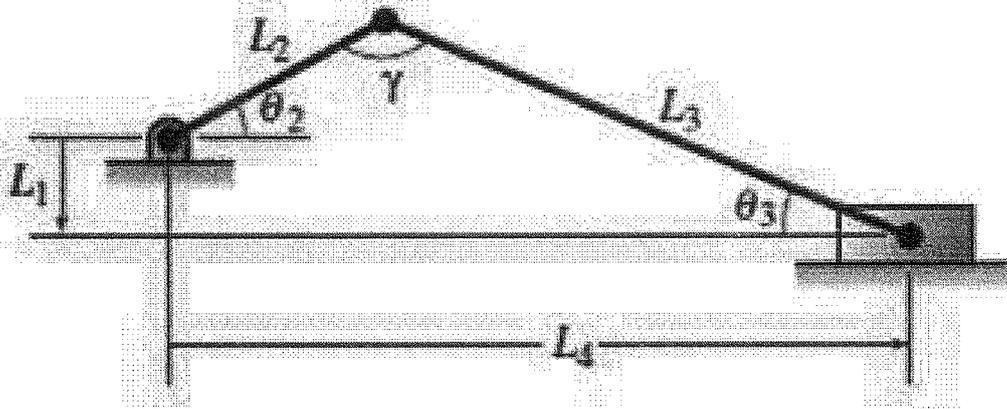
(d) Industrial Robotics

(e) Spatial Mechanism

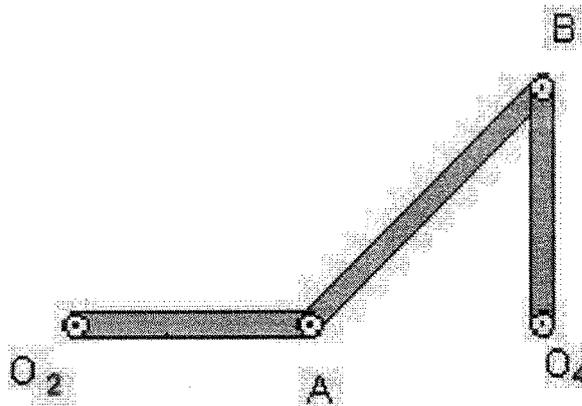


2. In the offset crank slider mechanism shown in the figure below the constrained path of the pin on the slider does not extend through the

center of rotation of the crank. Given the lengths  $L_1$ ,  $L_2$  and  $L_3$  and the crank angle  $\theta_2$ . Please determine (a) The interior joint angle  $\gamma$  and (b) The position of the slider  $L_4$ . (20%)

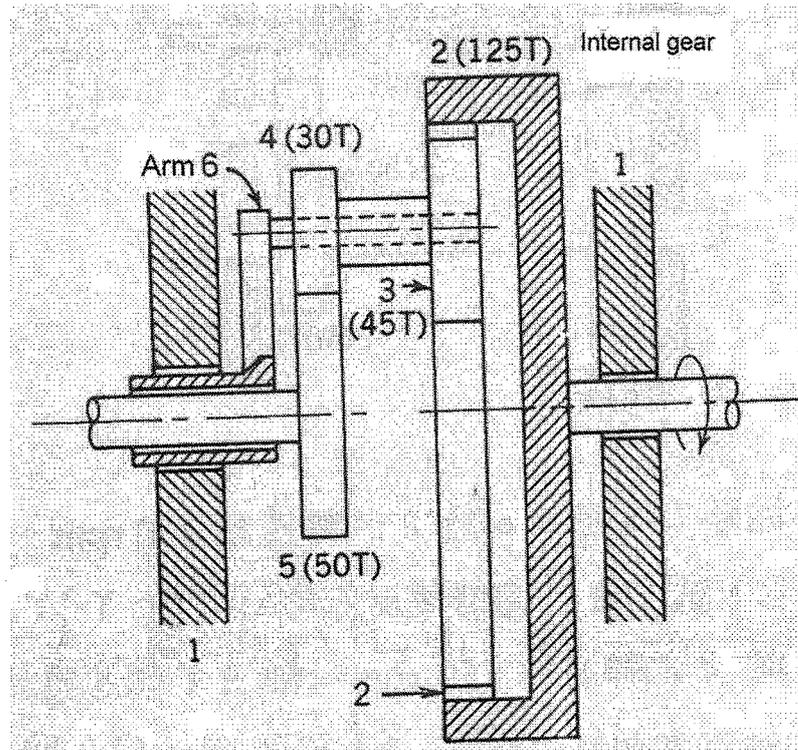


3. For the 4-bar linkage shown in the figure below, Link2 ( $O_2A$ ) rotates with the angular velocity  $\omega_2=10$  rad/s (CCW) and angular acceleration  $\alpha_2=10$  rad/s<sup>2</sup>. Given the lengths  $O_2O_4=2$ m (Link1: Fixed),  $O_2A=1$ m (Link2),  $O_4B=1$ m (Link4), and Link2 ( $O_2A$ ) overlaps with Link1 ( $O_2O_4$ ), Link4 ( $O_4B$ ) is perpendicular to Link1 ( $O_2O_4$ ). Please use any analytical method to calculate the angular velocities  $\omega_3$  and  $\omega_4$ , and the angular accelerations  $\alpha_3$  and  $\alpha_4$  of Link3 ( $AB$ ) and Link4 ( $O_4B$ ). (20%)



4. A 2-module,  $20^\circ$  pinion of 24 teeth drives a 40 teeth gear, calculate the pitch diameter, base radii, dedendum, addendum, tooth thickness on the pitch circle, circular pitch, length of action and the contact ratio. (20%)

5. In the planetary gear train shown in the Figure below, gear 2 turns at 600 rpm in the direction indicated. Determine the speed and direction of rotation of arm 6 if gear 5 rotates at 350 rpm in the same direction as gear 2. (20%)



國立虎尾科技大學 108 學年度第一學期博士班資格考試題

所別：機械與機電工程研究所

共 3 頁

科目：機構學

注意事項：

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- (2) 請依序作答於答案卷上並註明題號。
- (3) 可使用計算機。

1. For the mechanism as shown in Fig. 1 (a) and (b), please determine its degree of freedom, and give those in detail you need (such as: No. of links and joints, types of joints, etc.) for determining the degree of freedom

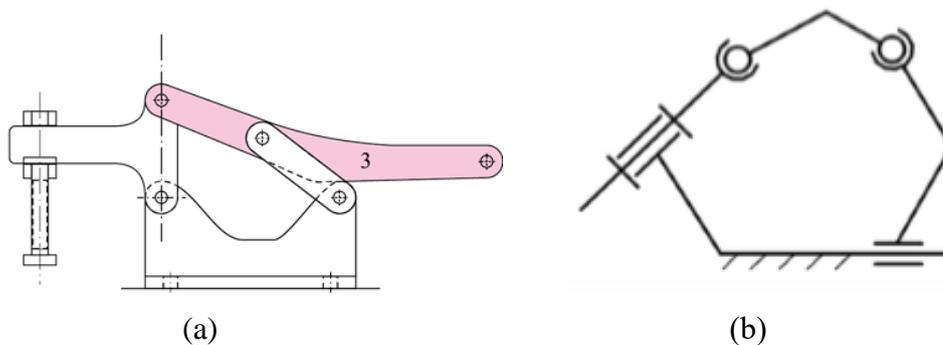


Fig. 1

2. Given  $r_1 = 10$  mm and  $r_3 = 25$  mm for a slider crank mechanism as shown in Fig. 2
  - (a) Determine the range of values of the length of link 2 so that link 2 can make a full rotation, and the transmission angle remains in the range  $45^\circ \leq \phi \leq 135^\circ$ .
  - (b) Continue from (a), determine the maximum stroke from the range of values of the length of link 2 you found in (a).

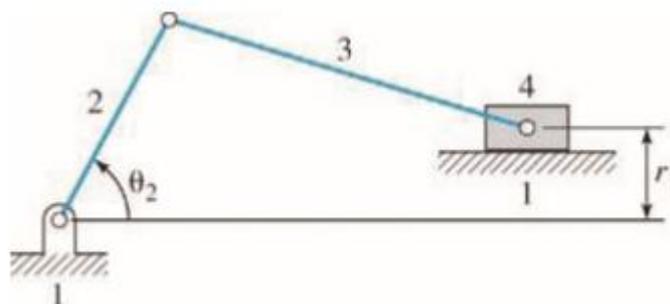


Fig. 2

3. For the mechanism as shown in Fig. 3, the origin of the coordinate system is on  $O_2$ , and the x axis is along the horizontal and directs to the right. The angular positions of links 2 and 3 are measured CCW from (positive) x axis. The distance between  $O_2$  and B is 5 cm, and that between B and C is 17 cm. If  $\theta_2 = 210^\circ$ , and  $\omega_2 = 60$  rad/sec CW (constant), please write the **vector equation** for the linkage shown and determine analytically the angular position, velocity, and acceleration of link 3.

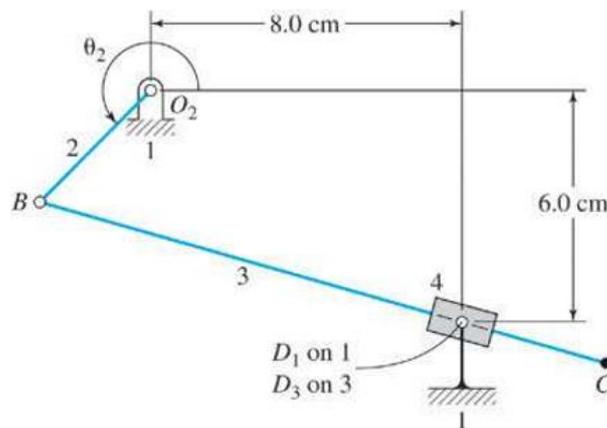


Fig. 3

4. In Fig. 4, the displacement–time, velocity–time, and acceleration–time curves are sketched for a follower. The cam rotates at a constant angular velocity  $\omega$  and the maximum (peak) value of the acceleration is 5 units. The equation for the acceleration-time curve is as follows

$$A = \left(\frac{2\pi h \omega^2}{\beta^2}\right) \sin\left(\frac{2\pi}{\beta} \phi\right)$$

- (a) Write the equations for the velocity-time and displacement–time curves.  
 (b) Determine the maximum values of displacement and velocity

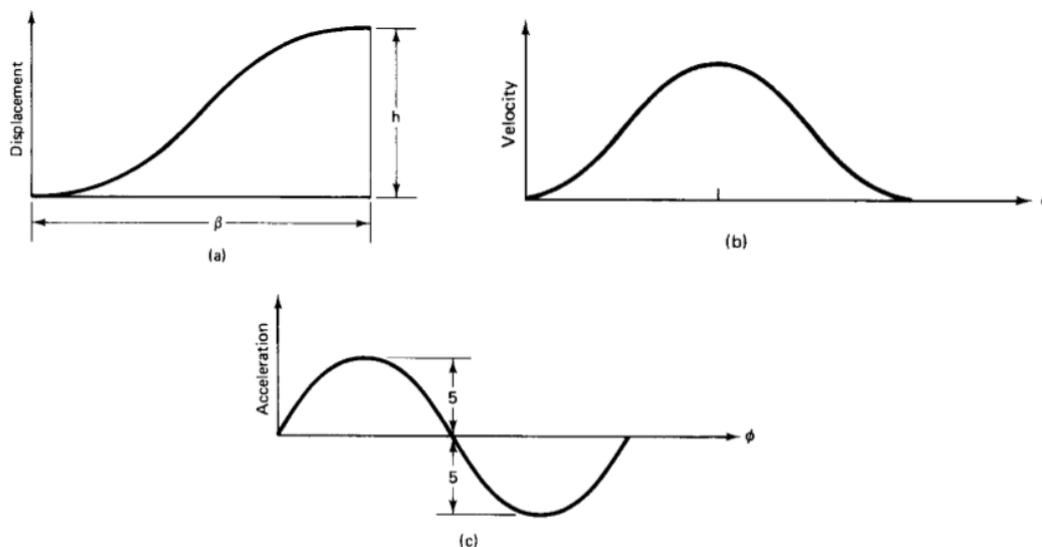
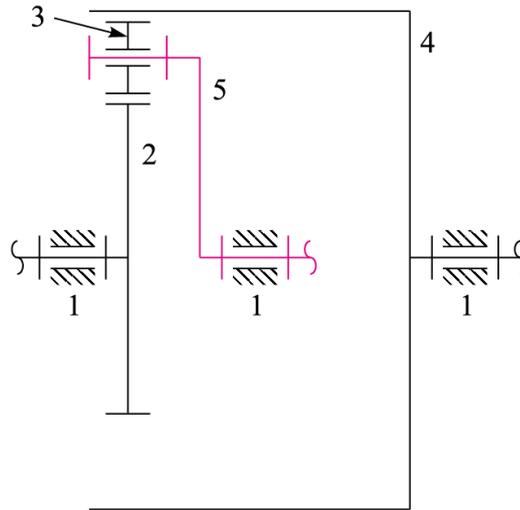


Fig. 4

5. The kinematic skeleton of the planetary gear train shown in Fig. 5(a) is shown in Fig. 5(b). This gear train has gear 2 as the sun gear ( $T_2 = 75$ ) and gear 3 as the planet gear ( $T_3 = 15$ ). Gear 4 is a ring gear ( $T_4 = 105$ ). Between gear 2 and gear 3 is carrier 5. Analyze the velocity ratios of this gear train.



(a)



(b)

Fig. 5

# 國立虎尾科技大學 107 學年度第二學期博士班資格考試題

所別：機械與機電工程研究所

共 3 頁

科目：機構學

注意事項：

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- (3) 可 使用計算機

1. Fig. 1 show a four-bar linkage, which is a crank-rocker mechanism. If  $r_2=100\text{cm}$ ,  $r_3=150\text{cm}$ ,  $r_4=200\text{cm}$ , please find the length range of  $r_1$ . (15%)

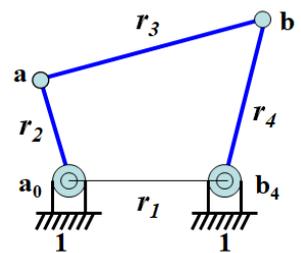


Fig.1. Four-bar linkage

2. Fig. 2 show an offset crank-slider. For the mechanism, if  $e=50\text{cm}$ ,  $r_2=200\text{cm}$ ,  $r_3=400\text{cm}$ , (a) Max. transmission angle and Min. transmission angle, (b) The stroke of this offset crank-slider. (15%)

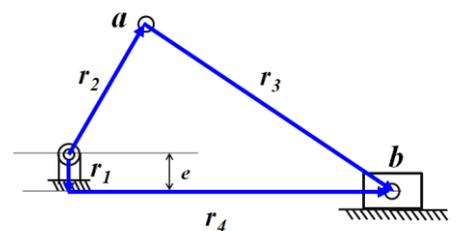


Fig. 2 An offset crank-slider

3. Fig. 3 show a four-bar linkage. For the mechanism, if  $r_1=180\text{cm}$ ,  $r_2=100\text{cm}$ ,  $r_3=150\text{cm}$ , and  $r_4 =200\text{cm}$ , (a) write down the vector loop equation, (b) if  $\theta_2=60^\circ$  and  $\omega_2=2400\text{rpm}$ , please find the values of  $\theta_3$ ,  $\theta_4$ , and transmission angle  $\mu$ , (c) if  $\omega_2=2400\text{rpm}$ , please find he values of  $\omega_3$  and  $\omega_4$ .(20%)

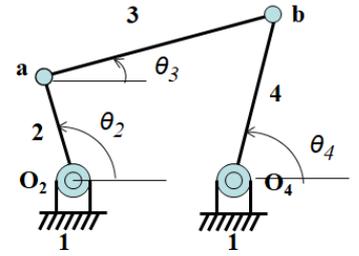


Fig.3. Four-bar linkage

4. For the mechanism shown m Fig.1, (a) please write down the vector loop equation, (b) find the close form equation for  $r_4$ , (c) if  $\theta_2 =60^\circ$  and  $\omega_2=2400\text{rpm}$ , please find  $r_4$ ,  $\theta_3$ ,  $V_b$ , and  $\omega_3$ .(20%)

5. Figs. 5(a) and 5(b) show two mechanisms. Please draw all instantaneous centers. (15%)

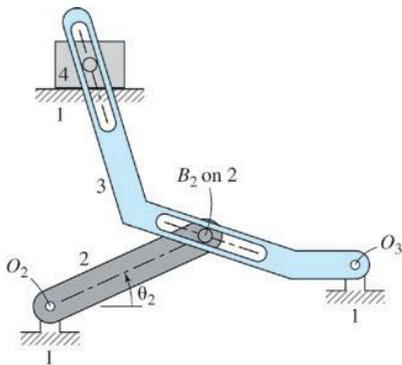


Fig. 5(a) Four-bar mechanism

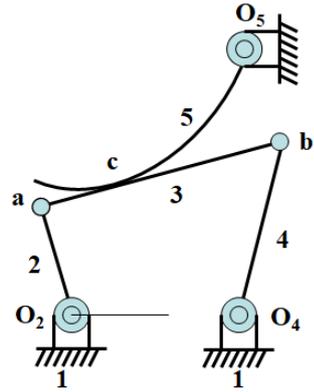


Fig. 5(b) Five-bar mechanism

6. Fig. 6 show a crank-slider. For the mechanism, if  $a_{a_o}=200\text{cm}$  ,  $a_{o_b}=400\text{cm}$  ,  $ad=800\text{cm}$  ,  $cd=600\text{cm}$  ,  $be=500\text{cm}$  , and  $\omega_2=100\text{ rad/s}$  . (a) According to the real dimensions of mechanism, please redraw this mechanism, (b) Using instant center method, find the angular velocity of link 3 ( $\omega_3$ ) and linear velocity of point c ( $V_c$ ). (15%)

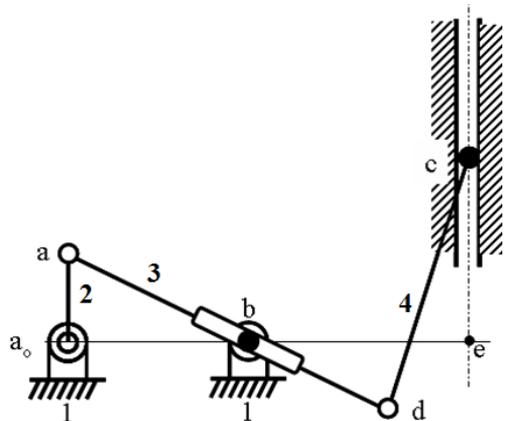


Fig. 6 Four-bar mechanism

# 國立虎尾科技大學 107 學年度第一學期博士班資格考試題

所別：機械與機電工程研究所  
 科目：機構學

共 3 頁

注意事項：

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 (3) 可 使用計算機

1. Figure 1 show a four-bar linkage. For the mechanism, if  $r_1=250\text{cm}$ ,  $r_2=100\text{cm}$ ,  $r_3=250\text{cm}$ , and  $r_4=150\text{cm}$ , (a) write down the vector loop equation, (b) if  $\theta_2 = 120^\circ$ , please find find the values of  $\theta_3, \theta_4$ , and transmission angle  $\mu$ . (20%)

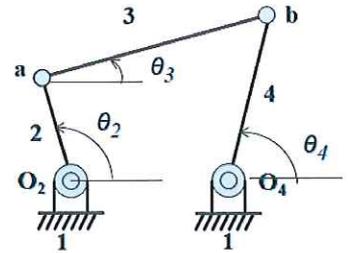


Fig.1. Four-bar linkage

2. Figure 2 show a offset crank-slider. For the mechanism, if  $e=2\text{cm}$ ,  $r_2=6\text{cm}$ ,  $r_3=10\text{cm}$ , (a) write down the vector loop equation, (b) find the close form equation for  $r_4$ , (c) if  $\theta_2 = 90^\circ$  and  $\omega_2=2400\text{rpm}$ , please find  $r_4$ ,  $\theta_3$ ,  $V_4$ , and  $\omega_3$ . (20%)

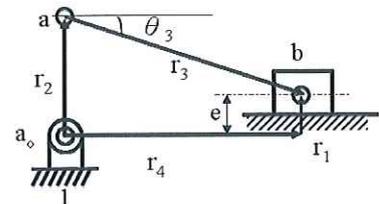


Fig. 2. Offset crank-slider

3. For a gear pair with module  $m=3.0$  and pressure angle  $\psi=14.5^\circ$ , a pinion ( $N_2=28$ ) drives a gear ( $N_3=72$ ). Please find (a) Contact length ( $L_c$ ), (b) Contact ratio ( $\gamma_c$ ). If center distance ( $C$ ) increases 1.5mm, please find (c) New pressure angle  $\psi'=?$ , (d) new Contact length ( $L_c'$ ), and (e) new Contact ratio ( $\gamma_c'$ ). (20%)

4. For a gear pair with module  $m=3.0$  and pressure angle  $\phi=14.5^\circ$ , if their addendums just pass the interference point and contact ratio ( $\gamma_c = 1.2348$ ), please find (a) Number of teeth  $N_2=N_3=?$ , (b) Addendum radius  $R_o$ . (20%)

5. Fig. 5 shows a gear reducer with ring gear 7 fixed. If sun gear 2 is the input link and sung gear 5 is the output link, if  $\omega_2=2400\text{rpm}$  (CCW), please find  $\omega_5$  (value and its direction).

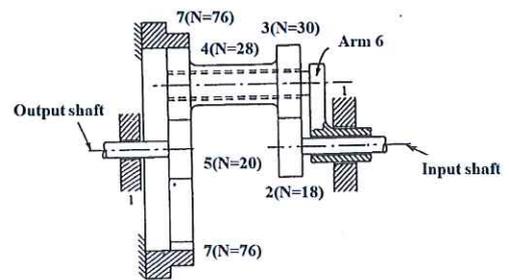


Fig.5. Planetary gear train

國立虎尾科技大學 104 學年度第一學期博士班資格考試題

所別：機械與機電工程研究所  
 科目：機構學 (可 使用計算機)

共 3 頁

1. Figures 1(a) and 1(b) show two mechanisms. Please draw all instantaneous centers. (20%)

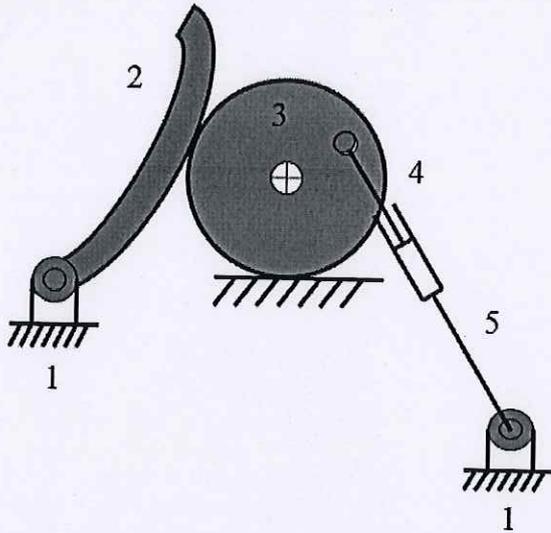


Figure 1(a) Five-bar mechanism

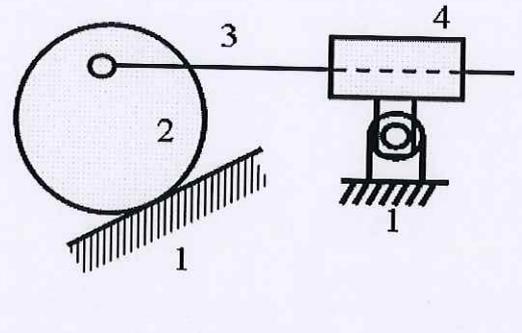


Figure 1(b) Five-bar mechanism

2. A four bar linkage as shown in Fig. 1,  $r_1=6\text{cm}$ 、 $r_2=2\text{cm}$ 、 $r_3=5\text{cm}$ 、 $r_4=5\text{cm}$ 、 $\theta_2 = 60^\circ$ . (a) According to the real dimensions of mechanism, please redraw this mechanism, (b) Please find  $\theta_3$  and  $\theta_4$ . (20%)

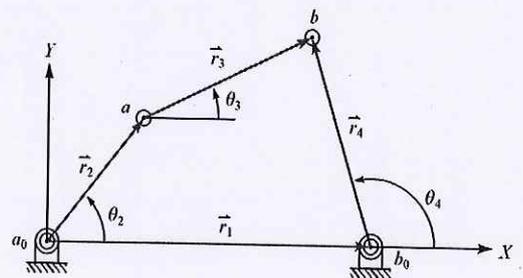


Fig. 1 Four-bar linkage

3. Figure 3 show a crank-slider. For the mechanism, if  $r_2=6\text{cm}$  ,  $r_3=4\text{cm}$  , and  $\theta_2=60^\circ$ . Using instant center method, find the linear velocity of slider 4 ( $V_C$ ). (20%)

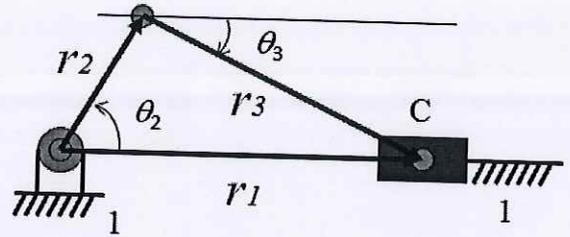


Figure 3 Slider-crank

4. For a planetary gear train as shown in figure 4, if  $\omega_2=1800\text{rpm}$  (CCW), please find the rotation speed of gear 5 and its rotation direction. (20%)

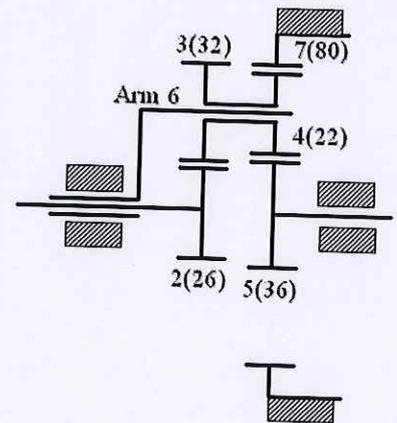


Figure 4 Planetary gear train

5. For a gear pair with module  $m=2.0$  and pressure angle  $\phi=20^\circ$ , a pinion( $N=21$ ) drives a gear ( $N=63$ ). Please find (a) Contact length ( $L_c$ ), (b) Contact ratio ( $\gamma_c$ ). If center distance ( $C$ ) increases  $0.08\text{mm}$ , please find (c) New pressure angle  $\phi'=?$ , (d) new Contact length ( $L'_c$ ) and Contact ratio ( $\gamma'_c$ ). (20%)

國立虎尾科技大學 101 學年度第一學期博士班資格考試題

所別：機械與機電工程研究所  
 科目：機構學 (可 使用計算機)

共 3 頁

1. Figure 1 shows a crank-rocker-slider mechanism. (a) Draw the corresponding specified kinematic chain. (b) Identify the link and joint types. (c) Identify the mobility number. (d) Calculate its degrees of freedom. (15%)

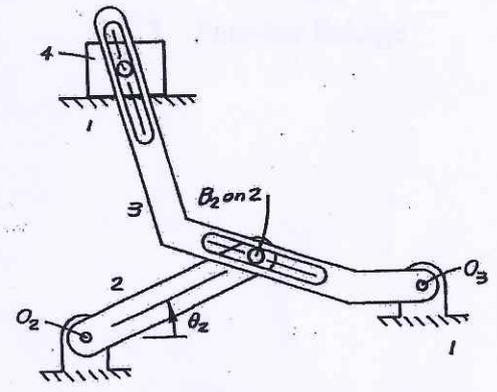


Figure 1 Crank-rocker-slider

2. Figures 2(a) and 2(b) show two mechanisms. Please draw all instantaneous centers. (20%)

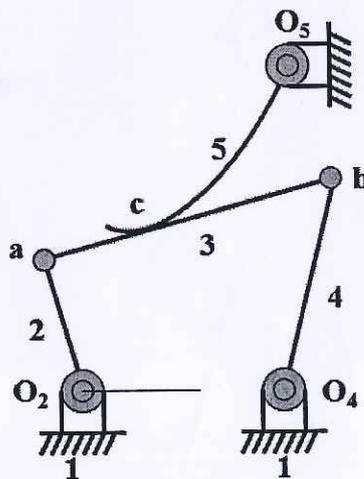


Figure 2(a) Five-bar mechanism

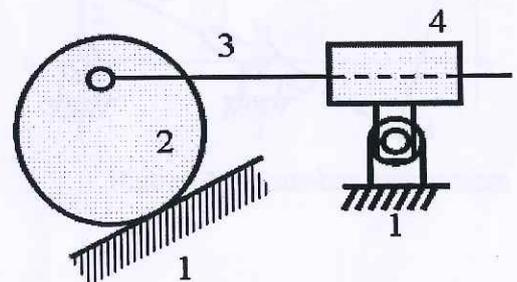


Figure 2(b) Five-bar mechanism

3. A four bar linkage as shown in Fig. 3,  $r_1$ 、 $r_2$ 、 $r_3$ 、 $r_4$ 、and  $\theta_2$  are given. Please find (a) and  $\theta_3$  and (b) when  $r_1=6\text{cm}$ 、 $r_2=2\text{cm}$ 、 $r_3=5\text{cm}$ 、 $r_4=5\text{cm}$ 、 $\theta_2=60^\circ$ , find the values of  $\theta_3$  and  $\theta_4$ . (15%)

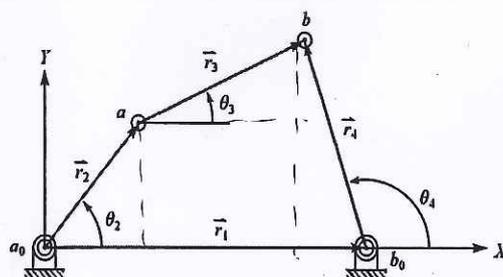


Fig. 3 Four-bar linkage

4. Figure 4 show a crank-slider. For the mechanism, if  $aa_0=2\text{cm}$ 、 $a_0b=4\text{cm}$ 、 $ad=8\text{cm}$ 、 $cd=6\text{cm}$ 、 $be=5\text{cm}$ 、and  $\omega_2=10\text{ rad/s}$ . (a) According to the real dimensions of mechanism, please redraw this mechanism, (b) Using instant center method, find the angular velocity of link 3 ( $\omega_3$ ) and linear velocity of point c ( $V_c$ ). (15%)

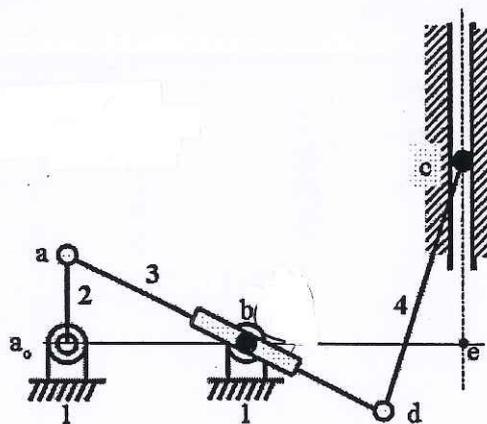
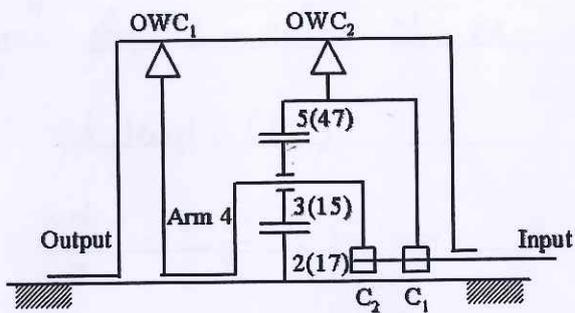


Figure 4 Four-bar mechanism

5. For the 3-speed internal gear hub shown in figure 5, please find the reduction ratios of the 3 speeds. (15%)



	C <sub>1</sub>	C <sub>2</sub>	OWC <sub>1</sub>	OWC <sub>2</sub>
1 <sup>st</sup> speed	⊙		⊙	Control not engaged
2 <sup>nd</sup> speed	⊙			⊙
3 <sup>rd</sup> speed		⊙		⊙

Figure 3 3-speed internal gear hub

⊙:Engaged

6. For a gear pair with module  $m=3.0$  and pressure angle  $\phi=20^\circ$ , a pinion ( $N=24$ ) drives a gear ( $N=72$ ). Please find (a) Contact length ( $L_c$ ), (b) Contact ratio ( $\gamma_c$ ). If center distance ( $C$ ) increases  $0.08\text{mm}$ , please find (c) New pressure angle  $\phi'=?$ , (d) new Contact length ( $L_c'$ ). (20%)

國立虎尾科技大學 103 學年度第一學期博士班資格考試題

所別：動力機械系機械與機電工程博士班

共 3 頁

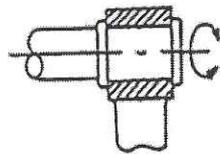
科目：機構學 (可使用計算機)

1. There are 9 kinematic pairs shown in figure 1. (20%)

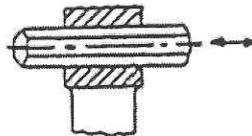
\_\_\_\_\_、\_\_\_\_\_、\_\_\_\_\_、\_\_\_\_\_ have 1 degrees of freedom.

\_\_\_\_\_、\_\_\_\_\_、\_\_\_\_\_ have 2 degrees of freedom.

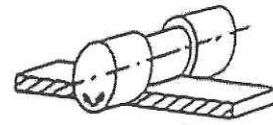
\_\_\_\_\_、\_\_\_\_\_ have 3 degrees of freedom.



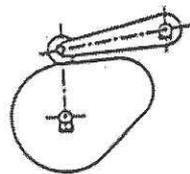
(a) Revolute pair



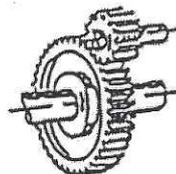
(b) Prismatic pair



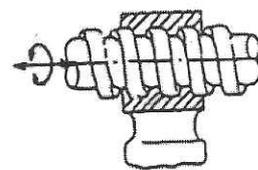
(c) Rolling pair



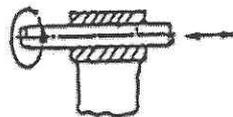
(d) Cam pair



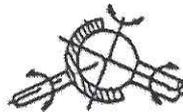
(e) Gear pair



(f) Helical pair



(g) Cylindrical pair



(h) Spherical pair



(i) Flat pair

Fig. 1 The kinematic pairs of mechanism

2. Figures 2(a) and 2(b) show two mechanisms. Please draw all instantaneous centers. (20%)

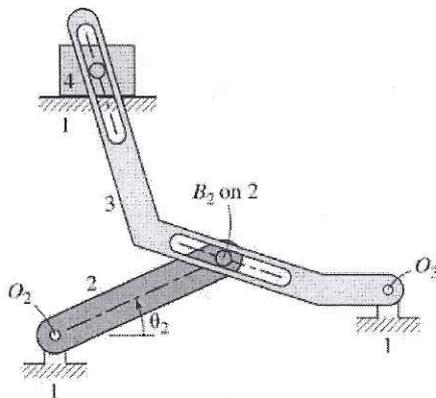


Fig. 2(a) Four-bar mechanism

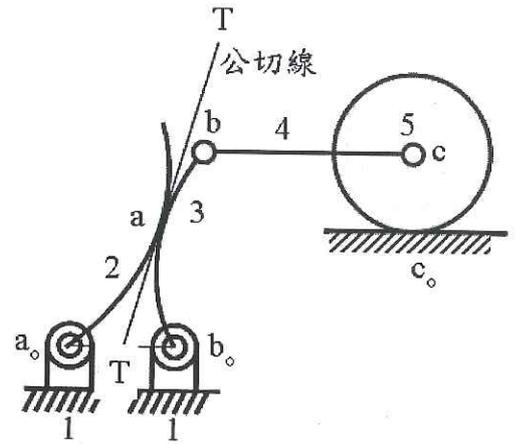


Fig. 2(b) Five-bar mechanism

3. Figure 3 show a offset crank-slider. For the mechanism, if  $aa_o=6\text{cm}$ ,  $ab=13\text{cm}$ , (a) write down the vector loop equation, (b) Find the close form equation for  $r_4$ , (c) please find  $r_4$  and  $\theta_3$  when  $\theta_2=90^\circ$ . (20%)

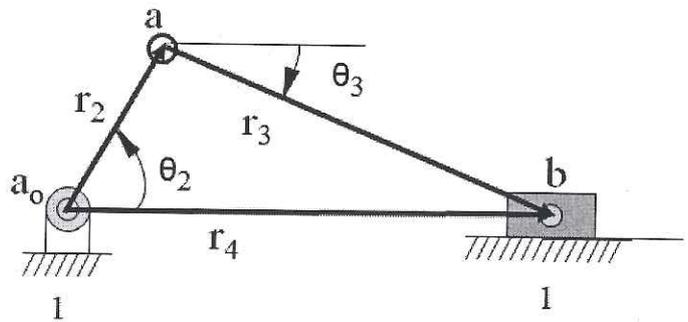


Figure 3 Offset crank-slider

4. For a gear pair with module  $m=2.0$  and pressure angle  $\phi=20^\circ$ , a pinion ( $N=24$ ) drives a gear ( $N=72$ ). Please find (a) Contact length ( $L_c$ ), (b) Contact ratio ( $\gamma$ ). If center distance ( $C$ ) increases  $0.05\text{mm}$ , please find (c) New pressure angle  $\phi'=?$ , (d) new Contact length ( $L_c'$ ). (25%)

5. For the planetary gear train shown in figure 5 (Ring gear 5 is fixed), if  $\omega_2=3600\text{rpm}$  (CCW), please find  $\omega_4$  (value and its direction). (15%)

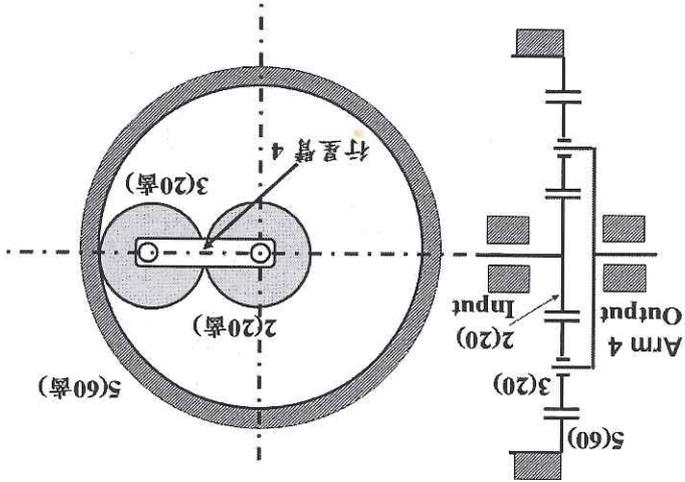


Fig. 5 Planetary gear train

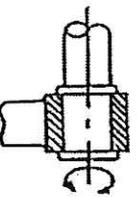
國立虎尾科技大學 102 學年度第二學期博士班資格考試題

所別：動力機械系機械與機電工程博士班

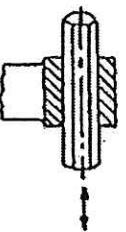
共 3 頁

科目：機構學 (可使用計算機)

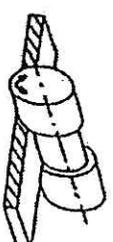
1. ( ) A (A)civil device (B)mechanical device (C)chemical device (D)electrical device is a piece of equipment, mechanical in nature, designed to serve a special purpose or perform a special function. It generally consists of mechanical members connected by joints. (5%)
2. ( ) Links can be classified based on the number of incident joints. A (A)singular (B)binary (C)ternary (D)quaternary link is one with three incident joints. (5%)
3. ( ) A (A)chain (B)power screw (C)belt (D)cam is an irregularly shaped link that serves as a driving member and imparts a prescribed motion to a driven link called follower. (5%)
4. ( ) In order to make mechanical members useful, they must be connected by joint (kinematic pair) The two members formed a kinematic pair are called (A)kinematic element (B)matching element (C)spouse element (D)pairing element. (5%)
5. ( ) For a prismatic or sliding pair, the relative motion between two incident members is (A)translation along an axis (B)rotation about an axis (C)the combination of rolling and sliding (D)pure rolling without slipping. (5%)
6. There are 9 kinematic pairs shown in figure 1. (10%)  
 \_\_\_\_\_, \_\_\_\_\_, \_\_\_\_\_ have 1 degrees of freedom.  
 \_\_\_\_\_, \_\_\_\_\_, \_\_\_\_\_ have 2 degrees of freedom.  
 \_\_\_\_\_, \_\_\_\_\_, \_\_\_\_\_ have 3 degrees of freedom.



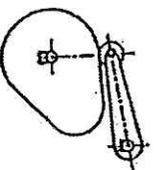
(a) Revolute pair



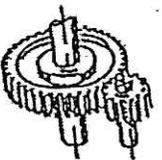
(b) Prismatic pair



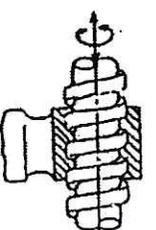
(c) Rolling pair



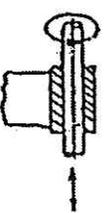
(d) Cam pair



(e) Gear pair



(f) Helical pair



(g) Cylindrical pair



(h) Spherical pair



(i) Flat pair

Fig. 1 The kinematic pairs of mechanism

7. Figures 2(a) and 2(b) show two mechanisms. Please draw all instantaneous centers. (20%)

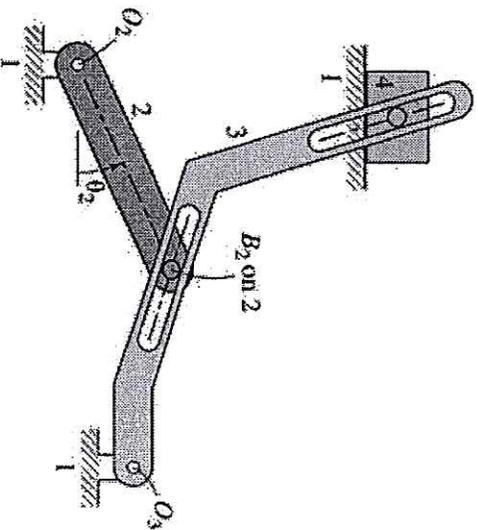


Fig. 2(a) Four-bar mechanism

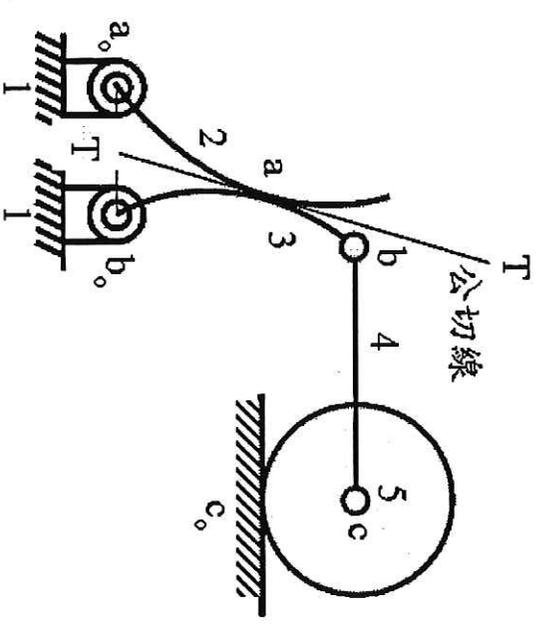


Fig. 2(b) Five-bar mechanism

8. Figure 3 show a offset crank-slider.  
 For the mechanism, if  $e=2\text{cm}$  ,  
 $a a_0=6\text{cm}$  ,  $ab=13\text{cm}$ , (a) write down the  
 vector loop equation, (b) Find the close  
 form equation for  $r_4$ , (c) please find  
 $r_4$  and  $\theta_3$  when  $\theta_2=90^\circ$ . (15%)

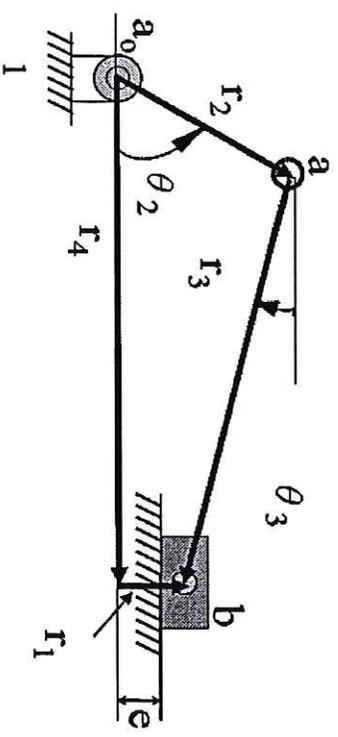


Figure 3 Offset crank-slider



一、有關機構自由度，請回答下列問題。

- (a) 解釋機構自由度的意義。(5%)
- (b) 說明機構自由度的計算式。(5%)
- (c) 試舉一例應證題(a)與題(b)。(10%)

二、如圖 1 所示，有一個牛頭刨床機構 (Crank-shaper mechanism)，桿長為已知。

$a_0b_0 = 3.0\text{cm}$ ， $a_0a = 1.5\text{cm}$ ， $b_0b = 6.0\text{cm}$ ， $bc = 3.5\text{cm}$ ， $b_0c = 6.0\text{cm}$  (垂直距離)，若桿 2 為輸入桿，即  $\theta_2 = 30^\circ$  (桿 2 與 x 軸夾角)， $\omega_2 = 10 \text{ rad/s}$  (ccw)， $\alpha_2 = 0 \text{ rad/s}^2$  為已知，請回答下列問題。

- (a) 利用繪圖法，求滑塊 c 的位置。(5%)
- (b) 以題(a)利用瞬心法求滑塊 c 的速度。(10%)
- (c) 利用向量迴路法求滑塊 c 的位置、速度、及加速度。(15%)

三、有關四連桿組，請回答下列問題。

- (a) 若桿 1、桿 2、以及桿 4 的長度分別為 300cm、100cm、以及 280cm，試求出耦桿 3 的長度  $r_3$  的範圍，使其為曲柄搖桿機構。(10%)
- (b) 承題(a)，若  $r_3=400 \text{ cm}$ ，試表示出曲柄搖桿機構的極限位置，並求出搖桿的運動範圍。(10%)
- (c) 承題(a)，若  $r_3=400 \text{ cm}$ ，試求出曲柄搖桿機構的最大與最小傳力角。(10%)

四、有關齒輪，請回答下列問題。

- (a) 何謂徑節(Diametral pitch)、何謂壓力角。(10%)
- (b) 如圖 2 齒輪系，若齒輪 6 固定，試求速比( $\omega_7/\omega_2$ )。(10%)

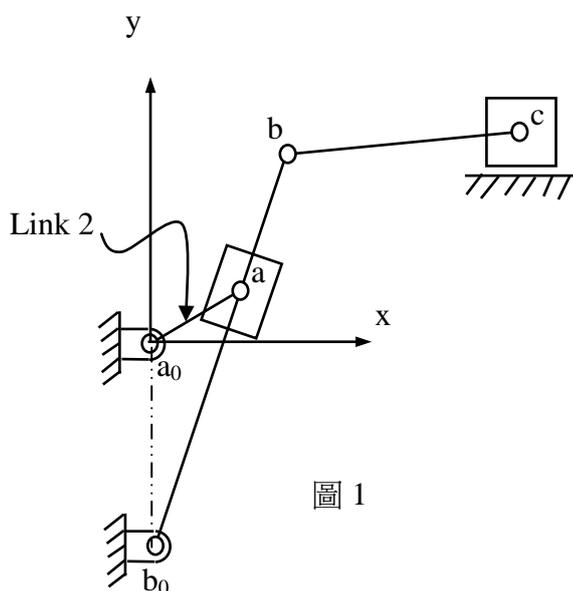


圖 1

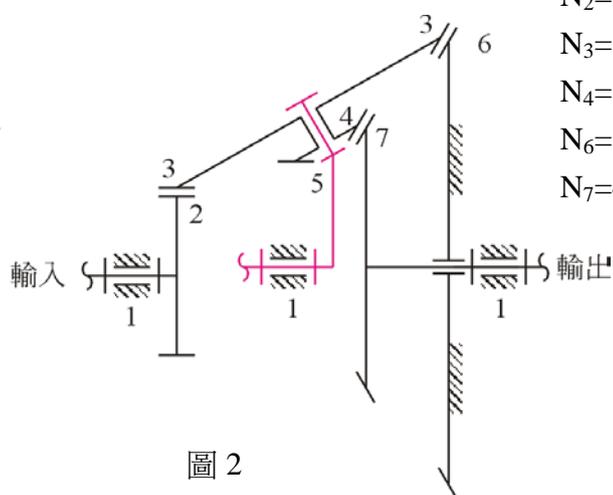


圖 2

各齒數：

$$N_2=16$$

$$N_3=64$$

$$N_4=30$$

$$N_6=80$$

$$N_7=40$$

1. Calculate the *DOF* of the linkages shown in Figure 1. (20%)

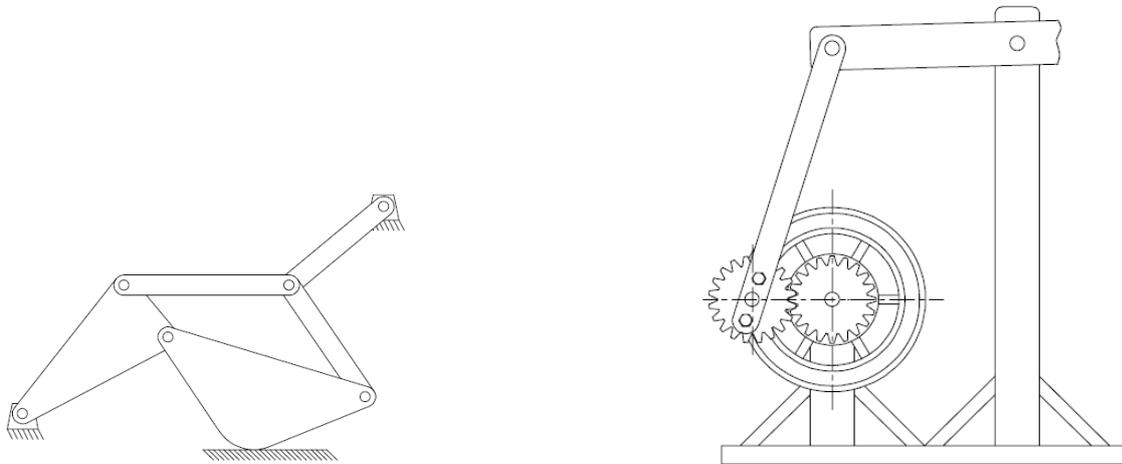


Figure 1

2. An inverted four-bar slider-crank linkage is shown in Figure 2. The length of input crank (link *a*)  $O_2A$  is 2.0 in and the angular velocities  $\omega_a = 10 \text{ rad/s}$  (c.c.w.). The length of coupler (link *c*)  $O_4B$  is 4 in. Using relative velocity method cooperates with velocity polygon method to find the velocities of the pin joints *A* and *B* and the velocity of slip at the sliding joint. Draw the linkage to scale. (30%)

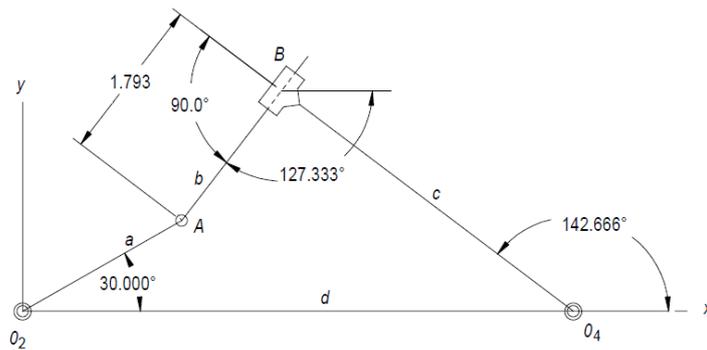


Figure 2 Fourbar slider-crank linkage

3. In the gear train of Figure 3, the inputs are the sun gear 5 and the ring gear 2. For given angular velocities of  $\omega_{s1} = 300 \text{ rpm}$  and  $\omega_{r1} = 500 \text{ rpm}$  (both counterclockwise as seen from the right), find the resulting rotation of ram 6. (25%)

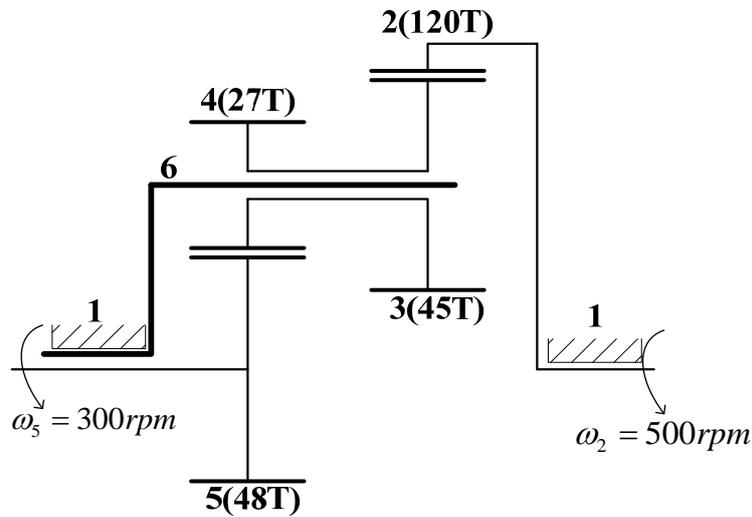


Figure 3 Gear train

4. Figure 4 shows a four-bar linkage. The angular velocity  $\omega_2 = 2 \text{ rad/s}$  (c.w.) of the input crank (link 2) is given; find the angular velocity of link 4 by using instant centers method. (25%)

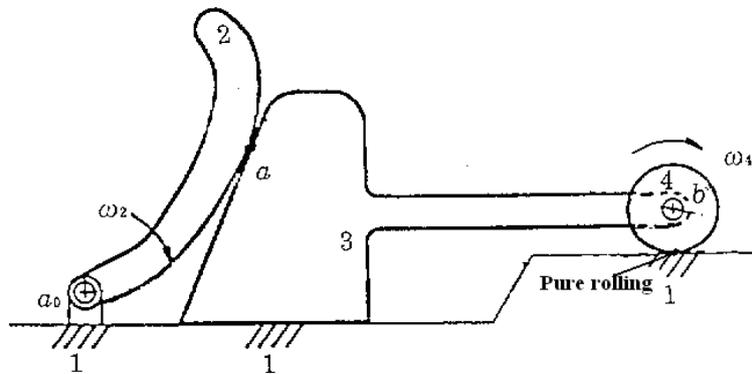


Figure 4 A four-bar linkage

\*Close book \*\* Answer in Chinese or in English \*\*\* Using a calculator is permitted

1. (a) Find the degrees of freedom of the mechanisms shown in Fig. 1a. (10%)

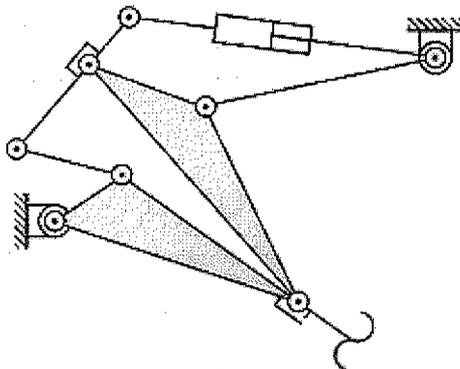


Fig. 1a

(b) Sketch the Structural sketch of the mechanism shown in Fig. 1b, and find its degrees of freedom. (10%)

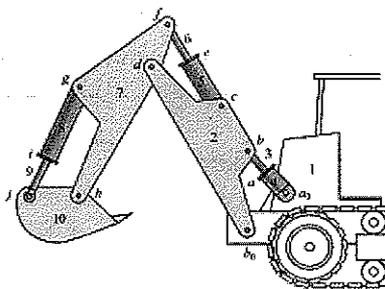


Fig. 1b

2. Fig. 5 shows a cam with a translating roller follower, derived its cam profiles by the envelope method. (20%)

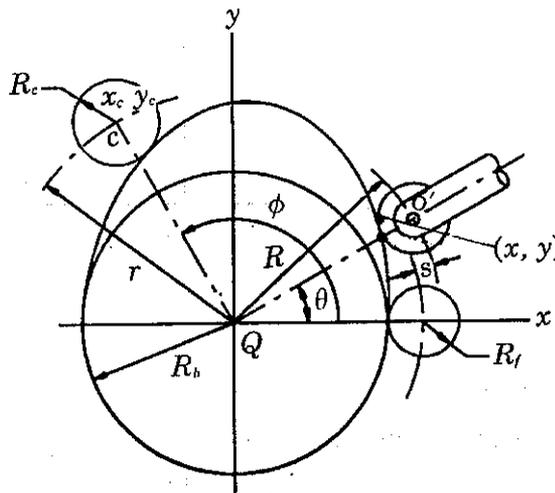


Fig. 2

3. Determine the speed ratio between the input shaft (gear 4) and the output shaft (arm 5) of the gear train shown in Fig. 3. Gear 2 is fixed, and the numbers of teeth for the gears are  $T_2=75$ ,  $T_3=15$ , and  $T_4=105$ , respectively, in the mechanism. (20%)

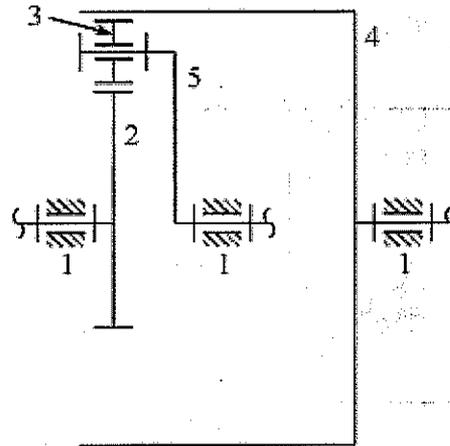


Fig. 3

4. Fig. 4 shows a crank-shaper crank mechanism, where Link 2 is the input. Find the closed form solution for the position of each link by using the vector loop closure approach. (20%)

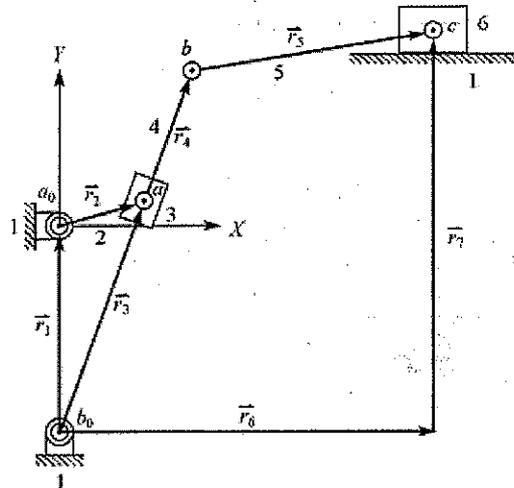


Fig. 4

5. Illustrate the following terms. (20%)
- (1) Toggle position
  - (2) Transmission angle
  - (3) Contact ratio of gearing
  - (4) Involute tooth profile and its interference

\*Close book \*\*Answer in Chinese or in English \*\*\* Using calculator is permitted

1. Calculate the degrees of freedom of the mechanisms shown in Fig. 1a and Fig. 1b. (20%)

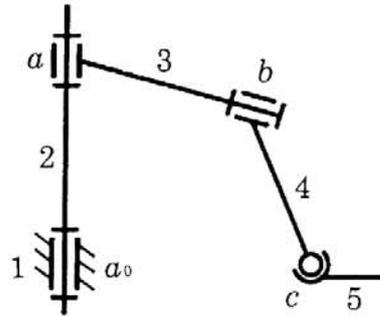


Fig. 1a

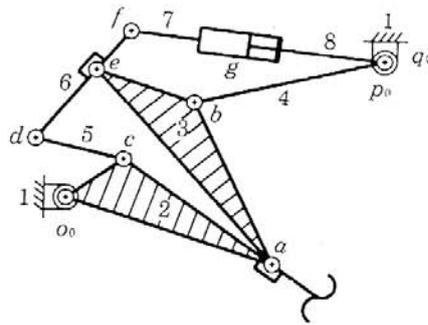
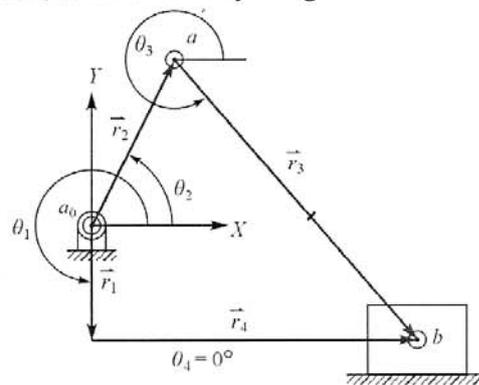


Fig. 1b

2. Fig. 2 shows a slider crank mechanism with the offset distance  $r_1$ , the lengths of link  $i$  ( $i=2-3$ ) are  $r_i$ . If link 2 is the input link, that is,  $\theta_2$  is given. In addition,  $\theta_1$  is  $270^\circ$ ,  $\theta_4$  is  $0^\circ$ . Find the closed form solution for the position  $r_4$  of the slider 4 by using the vector loop closure approach. (25%)



(b)

Fig. 2

3. Fig. 3 shows a slider crank mechanism with dimensions  $a_0a=10\text{cm}$ ,  $ab=30\text{cm}$ ,  $\theta_2 = 60^\circ$ . If the crank rotates at a constant angular velocity of  $\omega_2 = 100 \text{ rad/sec}$  (counterclockwise). (25%)
- (1) Find the angular velocity of the link 3 and the velocity of the slider 4. (10%)
- (2) Find the angular acceleration of the link 3 and the acceleration of the slider 4. (15%)

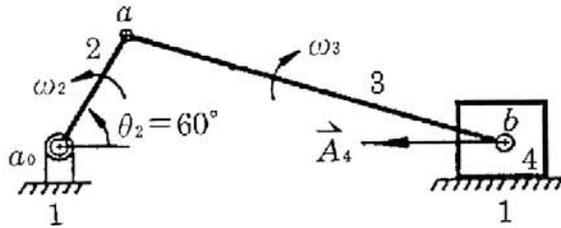


Fig. 3

4. Determine the speed ratio between the input and the output shafts of the gear train shown in Fig. 4, the numbers indicated in the figure are the number of teeth. (20%)

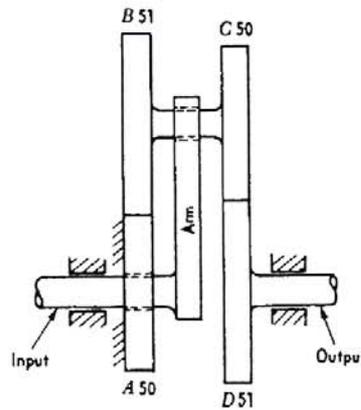


Fig. 4

5. Illustrate and explain the fundamental law of gearing. (10%)